

Here is a very short explanation of some of the symbols used in Chapter 2 of Eiben and Smith's book "*Introduction to Evolutionary Computing*". Courtesy of Maarten Lamers of the Media Technology MSc program, Leiden University.

- ε A symbol that is commonly used to denote some a-specific (very) small positive value. For example, $x = 1/(4 + \varepsilon)$ means that x is slightly smaller than $1/4$, such as $1/4.0001$. Actually, the typographic symbol used by Eiben and Smith is not exactly the same, but Microsoft Word does not support it.
- Δ A symbol that represents a change. For example Δw represents a change in value w .
- $\sum_{i=a}^b$ Summation over values $i \in a \dots b$. For example, if $a = 2$ and $b = 4$ then
$$\sum_{i=2}^4 (i \cdot 2) = \sum_{i=2}^4 (i \cdot 2) = (2 \cdot 2) + (3 \cdot 2) + (4 \cdot 2) = 18.$$
- $n!$ The faculty operator. For example, $5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 120$.
- $A \Rightarrow B$ B follows from A . This means that if statement A is true, then statement B is also true. For example, we know that $x \leq 5 \Rightarrow x < 9$.
- $\{\dots\}$ Represents a set, which is a collection of distinct items. For example, $P = \{1, 2, \dots, 9\}$ means that P is a set containing each of the integer numbers 1 through 9.

In the examples below, assume that set $P = \{1, 2, \dots, 9\}$.

- $p \in P$ Means that p is a member of set P . Given our example set P , p can be any of the integer values 1 through 9.
- $\{\dots | \dots\}$ Means *such that*. For example, $Q = \{q(p) \mid p \in P\}$ means that Q is the "set of all values $q(p)$ such that $p \in P$ ", or $Q = \{q(p) \mid p \in P\} = \{q(1), q(2), \dots, q(9)\}$. Another example: if N is the set of all natural numbers (integers) then, $\{2 \cdot x \mid x \in N\}$ is the set of all even natural numbers.
- $P \setminus G$ Set exclusion. For two sets P and G , $P \setminus G$ is the set containing all elements of P that are not in G . For example, if $G = \{3, 4, \dots, 99\}$ then $P \setminus G = \{1, 2, \dots, 9\} \setminus \{3, 4, \dots, 99\} = \{1, 2\}$.
- $(0,1)$ All possible real values between 0 and 1, *excluding* 0 and *excluding* 1.
- $[0,1)$ All possible real values between 0 and 1, *including* 0 but *excluding* 1.
- $(0,1]$ All possible real values between 0 and 1, *excluding* 0 and *including* 1.
- $[0,1]$ All possible real values between 0 and 1, *including* 0 and *including* 1.